



NAME

DATE

SOLUTION

PROBLEM: AP-7

GIVEN:

A rocket is fired from rest at $x = 0$ and travels along a parabolic trajectory described by $y^2 = [120(10^3)x]$ m. If the

x component of acceleration is $a_x = \left(\frac{1}{4}t^2\right)$ m/s², where t is in seconds, determine the magnitude of the rocket's velocity and acceleration when $t = 10$ s.

REQUIRED:

$$|v| = ?$$

$$|a| = ?$$

SOLUTION:

$$a_x = \frac{1}{4}t^2 \quad \int a_x dt = \int \frac{1}{4}t^2 dt \quad x = \frac{t^3}{12} \quad x = \frac{t^4}{48}$$

$$y^2 = 120E3x \quad y = \frac{120E3}{12}t^2 \quad y = 50t^2$$

$$\dot{y} = 100t \quad \ddot{y} = 100$$

at $t = 10$ s:

$$x = 208.3 \text{ m} \quad \dot{x} = 83.3 \text{ m/s} \quad \ddot{x} = 25 \text{ m/s}^2$$

$$y = 5000 \text{ m} \quad \dot{y} = 1000 \text{ m/s} \quad \ddot{y} = 100 \text{ m/s}^2$$

$$v = \sqrt{\dot{x}^2 + \dot{y}^2} = 1003.5 \text{ m/s}$$

$$a = \sqrt{\ddot{x}^2 + \ddot{y}^2} = 103.1 \text{ m/s}^2$$

$$|v| = 1004 \text{ m/s}$$

$$|a| = 103 \text{ m/s}^2$$